

# Federated Communication-Efficient Multi-Objective Optimization

Baris Askin

Pranay SharmaGauri JoshiCarnegie Mellon University

Carlee Joe-Wong



# Motivation

# Multi-objective Optimization (MOO)

- Single model optimized for multiple objectives
- Commonly used in practice, e.g., in recommender systems: relevance, diversity, safety, profit...

#### Federated Learning (FL)

- Train ML models with distributed data
- Heterogeneous data across clients
- Need for client data privacy



### **Proposed Method**

Federated Communication-Efficient MOO (FedCMOO)<sup>[3]</sup>

#### Initialize $\boldsymbol{x^0}$

For t = 0, ..., T - 1:

Server approximates w with  $\Theta(d)$  communication with clients  $(\star)$ Every active client i:

Trains a **single** model using the weighted objective  $\sum_k w_k f_{i,k}(x_i)$ Sends a **single** update,  $\Delta_i^t$ , to the server  $x^{t+1} \leftarrow x^t + Avg(\Delta_i^t)$ 

#### ( $\star$ ) How to approximate **w**:

1. Clients calculate a single stochastic gradient for each objective

#### **Federated Multi-Objective Optimization**

- Many real-world problems involve a federated setting and multiple objectives, e.g., in personalized medicine:
  - Multiple patients: diversity and privacy
  - Multiple objectives: precision, limited side-effects, cost-effectiveness...
- Underexplored in the literature

# **Problem: Federated MOO**

How can we design a communication- and time-efficient training for federated multi-objective models?

N clients and M objectives

Goal:  $\min_{\boldsymbol{x}\in\mathbb{R}^d} \boldsymbol{F}(\boldsymbol{x}) \coloneqq [F_1(\boldsymbol{x}), F_2(\boldsymbol{x}), \dots, F_M(\boldsymbol{x})]$ 

where global objectives are average of clients' local objectives:  $F_k(\boldsymbol{x}) = \frac{1}{N} \sum_{i=1}^{N} f_{i,k}(\boldsymbol{x}) \text{ for every } k \in [M]$  jective models?  $f_{1,1}(\mathbf{x})$   $f_{1,2}(\mathbf{x})$   $f_{N,1}(\mathbf{x})$  $f_{N,2}(\mathbf{x})$ 

- remember of a single stormastic gradient for each osjective
- 2. Compress them and send to the server (randomized-SVD)
- 3. The server averages them and updates  $\boldsymbol{w}$  with projected SGD

By finding objective weights w before local updates; Strength 1: Communication cost,  $\Theta(d)$ , does not scale with MStrength 2: Training a single model solves objective drift problem

# **Theoretical Guarantees**

#### Standard assumptions:

- Smoothness and bounded gradients
- Unbiased and bounded variance, bounded heterogeneity
- Unbiased compression operator

With an appropriate choice of learning rates, FedCMOO converges to a Pareto stationary solution: (see paper for details)

$$\frac{1}{T} \sum_{t=0}^{T-1} \mathbb{E} \left\| \sum_{k} w_{k}^{t} \nabla F_{k}(\boldsymbol{x}^{t}) \right\|^{2} \leq \mathcal{O}\left(\frac{1}{\sqrt{T}}\right)$$

The rate matches the best-known rate for single-objective FL

Sample complexity to achieve an $\epsilon$ -close solution (M: # of objectives)			
Work	Federated	Complexity	Non-standard Assumptions
SDMGrad <sup>[4]</sup>	X	$\mathcal{O}(M^2/\epsilon^2)$	✓ None
FSMGDA <sup>[2]</sup>	$\checkmark$	$\mathcal{O}(M^4/\epsilon^2)$	<b>X</b> Increasing batch size with $T$
Ours <sup>[3]</sup>	$\checkmark$	$\mathcal{O}(M/\epsilon^2)$	✓ None

#### $f_{1,M}(\boldsymbol{x}) \qquad \qquad f_{N,M}(\boldsymbol{x})$

# **Background and Baselines**

# $\begin{array}{l} \textbf{Multi-Objective Optimization}\\ \text{No } \pmb{x} \in \mathbb{R}^d \text{ simultaneously minimizes all objectives}\\ \text{Trade-off across objectives} \end{array}$



Goal: find a Pareto optimal  $\boldsymbol{x}$ 

If nonconvex, find a Pareto stationary  $\boldsymbol{x}$  that does not have a common descent direction for all objectives

#### **Baseline Methods** Multiple Gradient Descent Algorithm (MGDA)<sup>[1]</sup>:

- *Centralized*, iterative, and gradient-based MOO solver
- Every iteration:
  - Calculate all gradients,  $\{\nabla F_k(\boldsymbol{x})\}_{k=1}^M$
  - Find  $\mathbf{w}^* = \min_{\mathbf{w} \in S_M} \|\sum w_k \nabla F_k(\mathbf{x})\|$ , maximizing the minimum descent -  $\mathbf{x} \leftarrow \mathbf{x} - \eta \sum w_k^* \nabla F_k(\mathbf{x})$

# **Experimental Results and FedCMOO-Pref**

#### **Experimental Results**



Federated Stochastic MGDA (FSMGDA)<sup>[2]</sup>:

- No access to the full global gradients,  $\{\nabla F_k(\mathbf{x})\}_{k=1}^M$ . Every client *i*: - trains M models in parallel, one for each objective, with local SGD
  - sends model-sized updates,  $\{\Delta_{i,k}\}_{k=1}^{M}$ , for every objective to server
- The server averages the updates:  $\Delta_k^t \leftarrow Avg(\Delta_{i,k}^t)$ and find  $\mathbf{w}^* = \min_{\mathbf{w} \in S_M} \left\| \sum w_k \Delta_k^t \right\|$

Weakness 1: High,  $\Theta(Md)$ , communication cost Weakness 2: Drift across objectives' separate local trainings

### References

[1] Désidéri, et al. "Multiple-Gradient Descent Algorithm (MGDA) for Multiobjective Optimization," Comptes Rendus Mathematique, 2012.
[2] Yang, et al. "Federated Multi-Objective Learning," NeurIPS, 2023.
[3] Askin, et al., "Federated Communication-Efficient Multi-Objective Optimization," AISTATS, 2025.

[4] Xiao, et al. "Direction-Oriented Multi-Objective Learning: Simple and Provable Stochastic Algorithms," NeurIPS, 2023.

- **Communication-efficient** MOO framework in the federated setting
- Faster convergence by solving the objective drift problem
- Better convergence rate with milder assumptions
- FedCMOO-Pref: The first preference-based MOO for FL  $\,$

askinb.github.io for the full paper & code!